Exploring Relationship between Variables - Quiz $_{\rm Solutions}$

Question 1

What does the R command str() do?

- a. It generates a string of random numbers
- b. It strips any existing labels from a plot in R
- c. It provides information on the structure of an R object
- d. It stretches the y-axis on a graph to fit the data displayed

SOLUTION: c.

Question 2

How can you explore relationships between two numerical variables? (Note: Choose as many answers as you need)

- a. Correlation coefficent
- b. Scatter plot
- c. Box plot
- d. Shapiro Wilk test

SOLUTION: a. and b.

Question 3

What is the difference between the cor() and cor.test() commands in R?

SOLUTION: The cor() command computes only the correlation coefficient, while the cor.test() command also computes a hypothesis test for that coefficient. This means that the latter also includes a p-value you can use to judge how significant the correlation is.

Describe the relationship between the two variable in the following plot:



Relationship between age and length

SOLUTION: From this scatter plot, it looks like there is a strong, positive relationship between the age of a foetus and its length. In other words, as the age of a foetus increases, so does its length. The relationship looks very linear.

Describe the relationship between the two variable in the following plot:



Relationship between SIMD and crime rates

SOLUTION: From this scatter plot, it looks like there is a fairly strong, negative relationship between the SIMD crime rank and the SIMD crime count in 2012. In other words, as the crime rank increases, the crime count descreases. However, the relationship does not look entirely linear.

Question 6

Below is the R output for a correlation between precipitation (mm) and cucumber yield (kg/m2). Interpret the correlation coefficient.

[1] 0.8708738

SOLUTION: The correlation coefficient between precipitation and cucumber yield is 0.87. This indicates that there is a strong, positive linear relationship between the two variables. As the precipitation increases, so does the cucumber yield.

Below is the R output for a correlation between the weight and pulse rate of patients. Interpret the correlation coefficient.

[1] -0.2029782

SOLUTION: The correlation coefficient is -0.20. There thus seems to be a fairly weak linear relationship between a patient's weight and their pulse rate (i.e. as a patient's weight increases, their pulse rate decreases or vice versa). However, such a weak relationship might not be of much interest for further research.

Question 8

You have collected some data on cinema ticket sales and car accidents. You run a correlation in R and your correlation coefficient is 0.95. You conclude that watching movies causes car accidents. Is this a correct interpretation of a correlation coefficient? Please also provide a brief explanation for your chosen answer.

- Yes
- No

SOLUTION: The correct answer is no. Correlation does not equal causation and a correlation coefficient does not allow for any conculsions as to the causal relationship between two variables. A better interpretation would thus have been to say that there is a very strong, positive linear relationship between the variables. Another point to note is that this relationship might be due to another variables you have not considered in your study (such as bad weather).

Question 9

After running a correlation in R, you found that there is no linear relationship between the two numerical variables. Should you go ahead and perform a linear regression? Please also provide a brief explanation for your chosen answer.

- Yes
- No

SOLUTION: The correct answer is no. A linear regression assumes that there is a linear relationship between your variables. Therefore, if you already know that this is no the case, you should not perform a linear regression and instead choose a different test that is more suited to your data.

Question 10

What is the code to compute a linear regression in R? (Note: You may assume that the data set had been attached.)

- a. reg(dependent_variable ~ independent_variable)
- b. $lm(dependent_variable \sim independent_variable)$
- c. linear.reg(dependent_variable ~ independent_variable)
- d. l.regression(dependent_variable ~ independent_variable)

SOLUTION: b.

Interpret the intercept and coefficient of the following R output from a linear regression of the healing time (in days) of a wound in terms of the wound dimension (in mm):

```
##
## Call:
## lm(formula = wound$time ~ wound$dim)
##
## Residuals:
##
       Min
                1Q Median
                                ЗQ
                                       Max
## -14.340 -6.941
                    -1.724
                             6.159
                                    18.416
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                                               0.207
                 7.0837
                            5.5046
                                     1.287
## (Intercept)
## wound$dim
                 0.7063
                            0.0705
                                    10.017 1.12e-11 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 9.059 on 34 degrees of freedom
## Multiple R-squared: 0.7469, Adjusted R-squared: 0.7395
## F-statistic: 100.3 on 1 and 34 DF, p-value: 1.116e-11
```

SOLUTION: The slope is 0.71, so very every one unit increase in wound dimension (in this case, for every mm), the healing time for a wound increases by 0.71 days. The intercept is 7.08, which means that at a wound dimension of 0 mm, the healing time would be 7.08 days. Clearly, this interpretation does not make sense in the given example, as a non-existent would does not require any healing time. This likely due to the fact that the smallest wound in the sample was 30 mm and thus the predication for 0 mm in this particular regression is outwith the range of the data and thus very inaccurate. All in all, this means that here the interpretation of the intercept is not very meaningful.

Interpret the intercept and coefficient of the following R output from a linear regression of the length of a foetus (in cm) in terms of age (in days):

```
##
## Call:
## lm(formula = foetus$length ~ foetus$age)
##
## Residuals:
                  1Q
                      Median
##
       Min
                                    ЗQ
                                            Max
## -0.65506 -0.18972 0.01104 0.15364 0.72780
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.690881
                           0.148621
                                     -18.11
                                              <2e-16 ***
## foetus$age
               0.120455
                           0.002055
                                      58.62
                                              <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2655 on 82 degrees of freedom
## Multiple R-squared: 0.9767, Adjusted R-squared: 0.9764
## F-statistic: 3436 on 1 and 82 DF, p-value: < 2.2e-16
```

SOLUTION: The coefficient for age is 0.12, so for every one unit increase in age (in this case for every day) the lenghth of a foetus increases by 0.12 cm. The intercept is -2.69, which means that a foetus at age 0 would be -2.69 cm long. However, in this particular case interpreting the intercept does not make sense.

Interpret the intercept and coefficient of the following R output from a linear regression of the SIMD crime count in terms of the SIMD crime rank:

```
##
## Call:
## lm(formula = crimes$SIMD.Crime.2012.count ~ crimes$SIMD.Crime.2012.rank)
##
## Residuals:
##
     Min
              1Q Median
                            ЗQ
                                  Max
## -20.79 -7.75 -0.33
                          5.51
                                51.82
##
## Coefficients:
##
                                 Estimate Std. Error t value Pr(>|t|)
                                           2.5285067
                                                        27.95
## (Intercept)
                               70.6854678
                                                                <2e-16 ***
## crimes$SIMD.Crime.2012.rank -0.0127240 0.0006698
                                                      -19.00
                                                                <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 12.1 on 117 degrees of freedom
##
     (23 observations deleted due to missingness)
## Multiple R-squared: 0.7552, Adjusted R-squared: 0.7531
## F-statistic: 360.9 on 1 and 117 DF, p-value: < 2.2e-16
```

SOLUTION: The coefficient for the SIMD crime rank is -0.013. This means that for every one unit increase in crime rank, the crime count decreases by -0.013. The intercept is 70.69, which means that at crime rank 0 the crime count is 70.69. Interpreting this intercept only makes sense if there is a crime rank 0 on the SIMD.

Question 14

Why does it make sense to use summary(lm()) rather than just lm() when running a linear regression in R?

SOLUTION: Because lm() only computes the coefficients, while summary(lm()) provides you with a lot more information on the regression (including p-values and the coefficient of determination).

Question 15

Amend the following R code to make predictions not only for 100 but also for 200 and 500 without adding an additional line of code:

 $predict(lm(dependent_variable~independent_variable), newdata=data.frame(independent_variable=100), interval="pred")$

SOLUTION:

 $predict(lm(dependent_variable~independent_variable), newdata=data.frame(independent_variable=c(100, 200, 500)), interval="pred")$

Note: This code only works when the data set you are working with is attached.

Interpret the following predictions of exam scores (in %) for the average amount of sleep for 7 and 9.5 hours respectively:

##		fit	lwr	upr
##	1	51.34277	36.83852	65.84701
##	2	69.66099	55.09294	84.22905

SOLUTION:

The expected exam score for student who slept 7 hours, on average, is 51.34%. The expected exam score for student who slept 9.5 hours, on average, is 69.66%.

Question 17

What R code can be used to add a regression line (in the colour red) to the following plot:

```
activity <- read.table(file.choose(), header = TRUE, sep = ",")</pre>
```



Relationship Between Height and Weight

SOLUTION:

abline(lm(activity\$Weight ~ activity\$Height), col="red")

Interpret the coefficient of determination below for a regression of the lenth of a foetus in terms of age:

[1] 0.976694

SOLUTION: The coefficient of determination is 0.977, which means that 97.7% of the variability in the length of a foetus is explained by its age.